

CONTINUOUS INTERNAL EVALUATION- 3

Dept: BS	Sem / Div: II/A, B, C, D, E, F	Sub: Advanced Calculus and Numerical methods	S Code:18MAT21
Date:23-09-2021	Time: 9:30-11:00 am	Max Marks: 50	Elective: N
Note: Answer any 2 full questions, choosing one full question from each part.			

Q N	Questions	Marks	RBT	COs												
PART A																
1 a	Form the partial differential equation by eliminating the arbitrary constants from $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$	8	L1	CO3												
b	Solve $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$, for which $\frac{\partial z}{\partial y} = -2 \sin y$ when $x=0$ and $z=0$ when y is an odd multiple of $\frac{\pi}{2}$	8	L2	CO3												
c	Solve one dimensional wave equation, using the method of separation of variables.	9	L3	CO3												
OR																
2 a	Form the partial differential equation by eliminating the arbitrary function from $f(x^2 + y^2, z - xy) = 0$	8	L1	CO3												
b	Solve $\frac{\partial^2 z}{\partial y^2} = z$, given that when $y=0, z=e^x$ and $z=e^{-x}$	8	L2	CO3												
c	Solve one dimensional heat equation, using the method of separation of variables.	9	L3	CO3												
PART B																
3 a	Apply Newtons backward difference formula to find $y(3)$ given that <table border="1" style="margin: 5px auto; border-collapse: collapse;"> <tr> <td style="padding: 2px 10px;">x</td> <td style="padding: 2px 10px;">-4</td> <td style="padding: 2px 10px;">-2</td> <td style="padding: 2px 10px;">0</td> <td style="padding: 2px 10px;">2</td> <td style="padding: 2px 10px;">4</td> </tr> <tr> <td style="padding: 2px 10px;">y</td> <td style="padding: 2px 10px;">-25</td> <td style="padding: 2px 10px;">1</td> <td style="padding: 2px 10px;">3</td> <td style="padding: 2px 10px;">29</td> <td style="padding: 2px 10px;">127</td> </tr> </table>	x	-4	-2	0	2	4	y	-25	1	3	29	127	8	L2	CO5
x	-4	-2	0	2	4											
y	-25	1	3	29	127											
b	Use Newton-Raphson method to find the real root of the equation $x \sin x + \cos x = 0$ near $X = \pi$. Carry out iterations up to 4 decimal places of accuracy.	8	L3	CO5												
c	Evaluate $\int_4^{5.2} \log_e x dx$, taking 6 equal strips by applying Weddle's rule	9	L2	CO5												
OR																

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4	a	Using Newtons divided difference formula evaluate f(8) given						8	L3	CO5	
		x	4	5	7	10	11				13
		y	48	100	294	900	1210				2028
	b	Find a real root of the equation $x \log_{10} x = 1.2$ by Regula Falsi method correct to four decimal places.						8	L3	CO5	
	c	Evaluate $\int_0^{\frac{\pi}{2}} \sqrt{\sin x} dx$ using Simpson's $(\frac{1}{3})^{rd}$ rule, taking 10 equal parts.						9	L2	CO5	